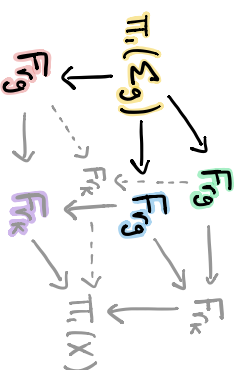


GROUP TRISECTIONS AND SMOOTHLY KNOTTED SURFACES

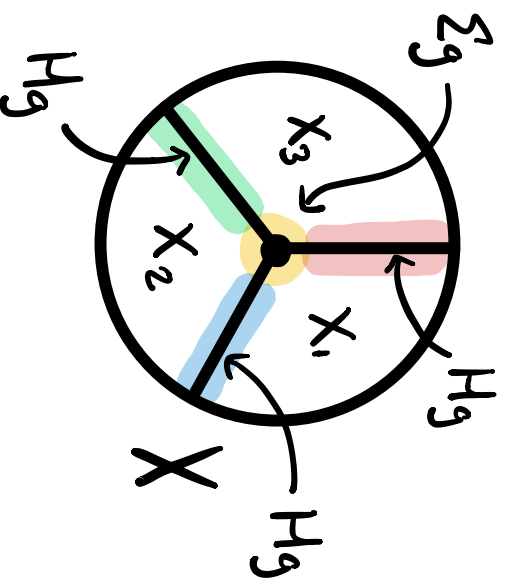
Sarah Blackwell

University of Georgia

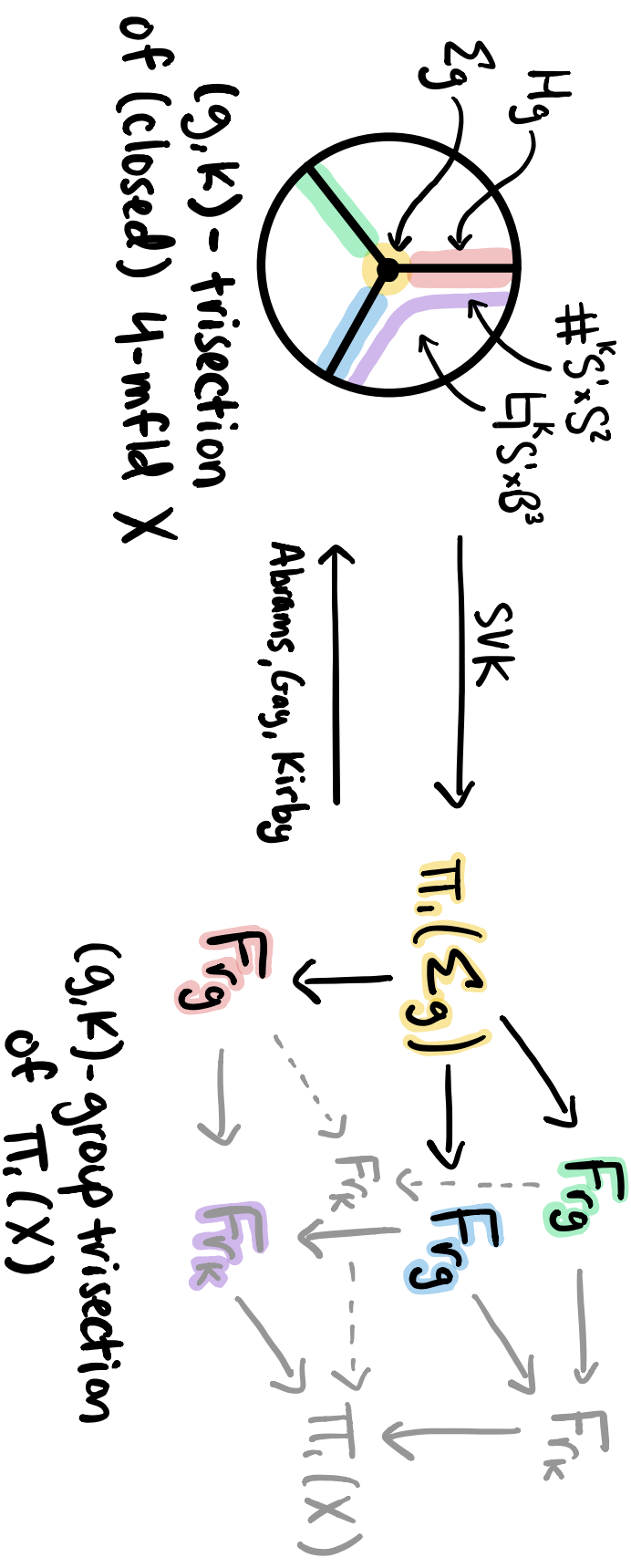
J.W. Kirby, Klug, Longo, Ruppik



(g, k) -trisection
of (closed) 4-mfld $X = \text{decomposition } X = X_1 \cup X_2 \cup X_3$ st
[Gay + Kirby]



- 1) $X_i \cong \mathbb{D}^k(S^1 \times B^3)$
- 2) $X_i \cap X_j \cong H_g$
- 3) $X_1 \cap X_2 \cap X_3 \cong \Sigma_g$



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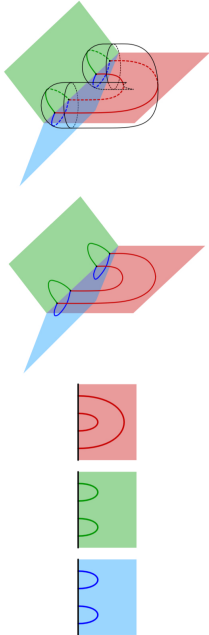
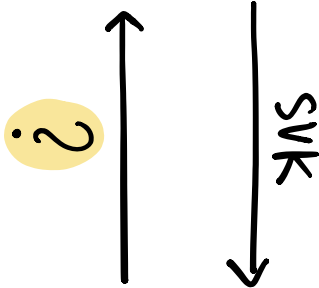


FIGURE 4. A 2-bridge trisection of an unknotted 2-sphere, depicted with the tri-plane in 3-space, along with the corresponding tri-plane diagram.

bridge trisection for
a surface in S^4
[Meier + Zupan]



$$\begin{array}{c}
 \pi_1(\beta_3^3 \setminus \alpha) \longrightarrow \pi_1(S_3^3 \setminus \mathcal{U}_{\beta^x}) \\
 \nwarrow \quad \downarrow \quad \nearrow \\
 \pi_1(S^2 \setminus 2b^*) \longrightarrow \pi_1(\beta_2^3 \setminus \beta) \longrightarrow \pi_1(S^4 \setminus S) \\
 \downarrow \quad \quad \quad \downarrow \quad \quad \quad \downarrow \\
 \pi_1(\beta_1^3 \setminus \alpha) \longrightarrow \pi_1(S_1^3 \setminus \mathcal{U}_{\alpha\beta}) \longrightarrow \pi_1(S_1^4 \setminus \mathcal{D}_{\alpha\beta}) \\
 \cong \pi_1(\beta_1^4 \setminus \mathcal{D}_{\alpha\beta})
 \end{array}$$

Van Kampen diagram for the
complement of a surface S in S^4

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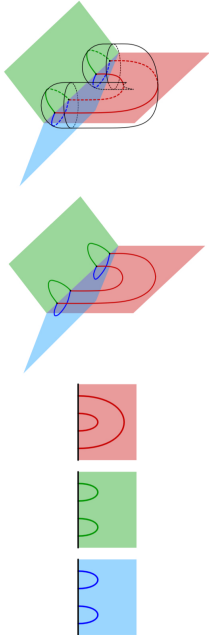
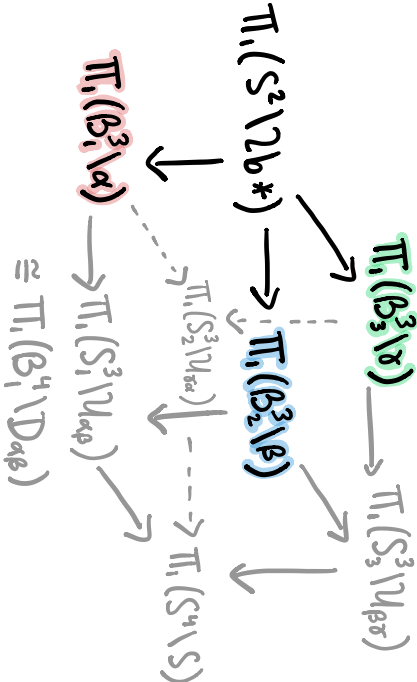
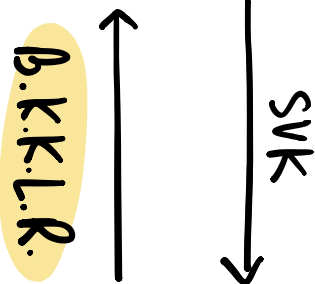


FIGURE 4. A 2-bridge trisection of an unknotted 2-sphere, depicted with the tri-plane in 3-space, along with the corresponding tri-plane diagram.

bridge trisection for a surface in S^4
[Meier + Zupan]



Van Kampen diagram for the complement of a surface S in S^4